

Finite Element Analysis Report by CANDE (Culvert Analysis and Design)

## Arroya Crossing Timber Ridge

Merlin# 723523

Colorado Springs, CO

November 10, 2022

The purpose of this report is to present the study of how a BridgeCor structure is expected to behave with the site conditions including soils information. A CANDE analysis was performed assuming the soil conditions based on provided information and some assumptions, which are summarized on the following pages. This report will examine: combined thrust and moment, seam strength, wall area, global buckling, and deflection, and unfactored footing reactions. The analysis was in accordance with the AASHTO LRFD Bridge Design Specification.

### Structure:

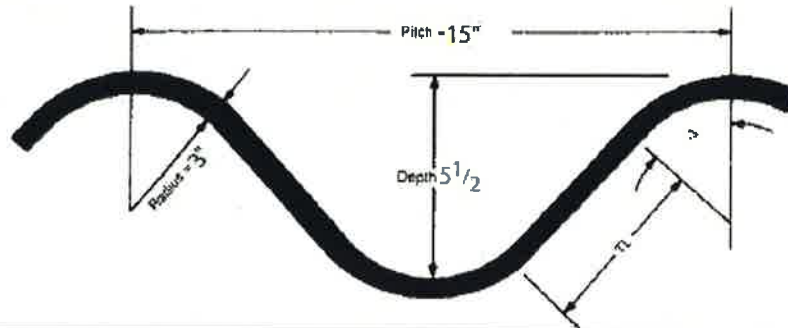
Bottom Span: 31'-10"  
Rise: 11'-8"  
Design cover: 4'-0"  
Gage: 8

### Summary:

- a. Load Factors: 1.75 for Live Load and 1.50 for Dead Load
- b. Modified Load Factors: 1.05 for Live Load (Multiple Presence Factor)
- c. For this structure, HL-93 design truck (32,000 pound axles spaced at 14 feet) and HL-93 tandem (25,000 pound axles spaced at 4 feet) loading were used as live load. The HL-93 design truck governed. As required by AASHTO, the combination of loads was the factored Dead Load plus the factored Live Load, which is determined as the controlling load case.
- d. Resistance Factors: Plastic Hinge Resistance Factor ( $\phi_h$ ) = 0.90, Wall Area and Buckling Resistance Factor ( $\phi_w$ ) = 0.70, Seam Strength Resistance Factor ( $\phi_{SS}$ ) = 0.67.
- e. Properties: Area of the Wall Cross-Section = 0.2302 in.<sup>2</sup>/in., Moment of Inertia = 0.8746 in.<sup>4</sup>/in., Section Modulus = 0.2884 in.<sup>3</sup>/in., Plastic Section Modulus = 0.4030 in.<sup>3</sup>/in.
- f. Profile of the BridgeCor deep corrugated plate (See next page for profile and data table). Profile is 15" Pitch and 5.5" Depth.
- g. Density of the backfill soil on top of the structure = 120 pcf (pounds per cubic foot)
- h. Density of the soil outside of the excavation of the arches = 120 pcf (pounds per cubic foot)
- i. Calculations of the Live loads, dead loads, etc.: See the following summary report.



**Product Details and Fabrication**



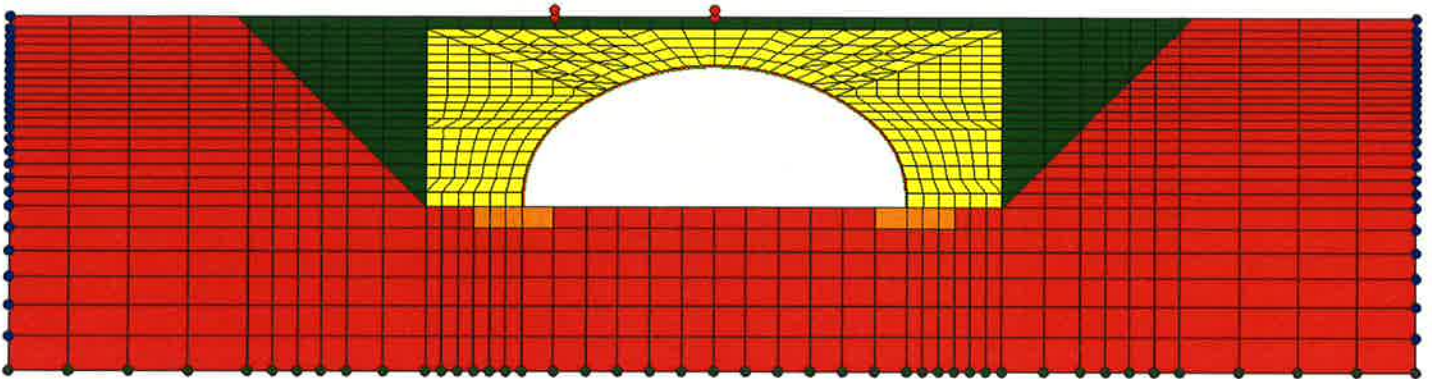
**Table 2.14**

**Sectional properties of 15 x 5 1/2 in. (Annular)**

Specified Thickness	Uncoated Thickness <i>t</i>	Area of Section <i>A</i>	Tangent Length <i>TL</i>	Tangent Angle <i>Δ</i>	Moment of Inertia <i>I</i>	Section Modulus <i>S</i>	Radius of Gyration <i>r</i>	Developed Width Factor
(in.)	(in.)	(in. <sup>2</sup> /ft)	(in.)	(Degrees)	(in. <sup>4</sup> /in)	(in. <sup>3</sup> /ft)	(in.)	
0.140	0.1345	2.260	4.361	49.75	0.7146	2.8406	1.9481	1.400
0.170	0.1644	2.762	4.323	49.89	0.8746	3.4602	1.9494	1.400
0.188	0.1838	3.088	4.299	49.99	0.9786	3.8599	1.9502	1.400
0.218	0.2145	3.604	4.259	50.13	1.1436	4.4888	1.9515	1.400
0.249	0.2451	4.118	4.220	50.28	1.3084	5.1114	1.9527	1.400
0.280	0.2758	4.633	4.179	50.43	1.4722	5.7317	1.9540	1.400
0.193	0.1875	3.150	4.293	50.00	0.9985	3.9359	1.9503	1.400
0.255	0.2500	4.200	4.213	50.31	1.3349	5.2107	1.9529	1.400
0.318	0.3125	5.250	4.131	50.62	1.6730	6.4678	1.9555	1.400
0.380	0.3750	6.300	4.047	50.94	2.0128	7.7076	1.9580	1.400

- Notes: 1. Per foot of projection about the neutral axis.  
 To obtain *A* or *S* per *inch* of width, divide the above values by 12.  
 2. Developed width factor measures the increase in profile length due to corrugating.  
 Dimensions are subject to manufacturing tolerances.

CANDE Generated Cross Section



Two Radius Arch Bridge Cor: 33S 31'-10" Span x 11'-8" Rise (Inside Dimensions) Gage: 8

Height of cover above crown: 4'-0"

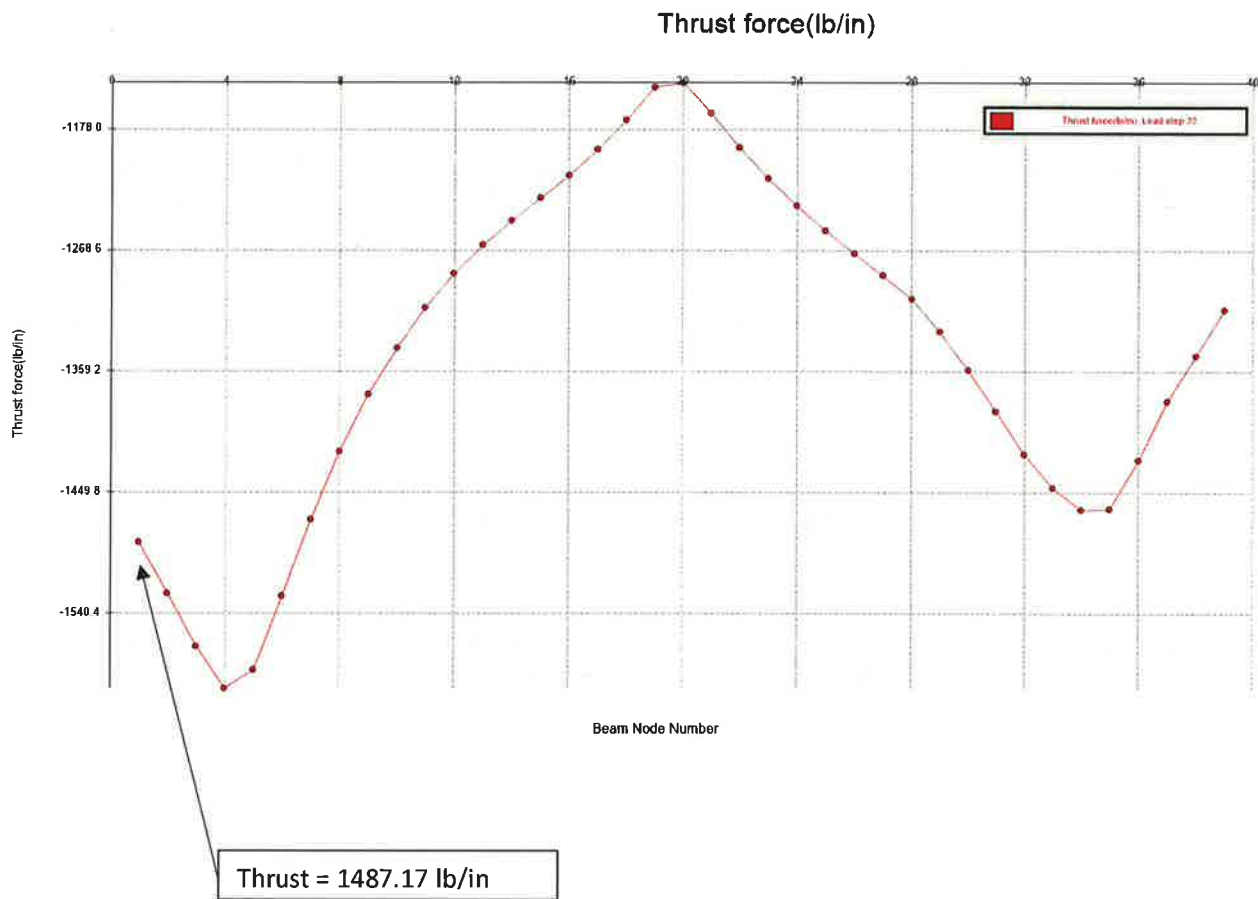
- Red mesh: Assumed: Isotropic-linear elastic, Young's modulus = 3,000 psi, Poisson's ratio = 0.30, density = 1 pcf (Density assumed to be 1 pcf to represent existing, consolidated soil – modeled to approximate no displacement)
- Green mesh: Embankment fill (assumed): Duncan/Selig SM90 , Density = 120 pcf
- Yellow mesh: Select backfill (assumed): Backfill width = 8'-0", Duncan/Selig SW95, Density = 120 pcf
- Orange mesh: Reinforced concrete footing (assumed): Isotropic-linear elastic, Young's modulus = 3,500,000 psi, Poisson's ratio = 0.18, Density = 150 pcf
- Green boundary point: Displacement restricted in the vertical direction
- Blue boundary point: Displacement restricted in the horizontal direction
- Red boundary point: Force above crown of arch representing 32,000 pound HL-93 Truck live load

**\*Design Criterion Summary:**

- Wall Thrust Resistance Ratio =  $31.06 / 85.1 = 0.365 < 1.00$  **OK**
- Global Buckling Resistance Ratio =  $2.58828 / 8.17 = 0.317 < 1.00$  **OK**
- Seam Thrust Resistance Ratio =  $31.06 / 59.63 = 0.521 < 1.00$  **OK**
- Combined Thrust & Moment Ratio =  $0.424 < 1.00$  **OK**

\*See sections below for more on calculations

CANDE Unfactored Thrust Reactions



Base Angle: -4.955 degrees

Unfactored Vertical Footing Reaction:  $R_v = \cos(-4.955) \times 1487.17 \times 12 = 17,779 \text{ lbs/ft}$

Unfactored Horizontal Footing Reaction:  $R_H = \sin(-4.955) \times 1487.17 \times 12 = -1,541 \text{ lbs/ft}$

Notes:

- Each node represents a location along perimeter of cross-section
- Unfactored reactions are for each leg

**AASHTO 12.8.9.5 (Combined Thrust & Moment Resistance)** requires deep-corrugated metal plate structures to be analyzed using a finite element analysis. The results from the analysis are then used to compute a combined thrust and moment ratio (Combined T&M Ratio):

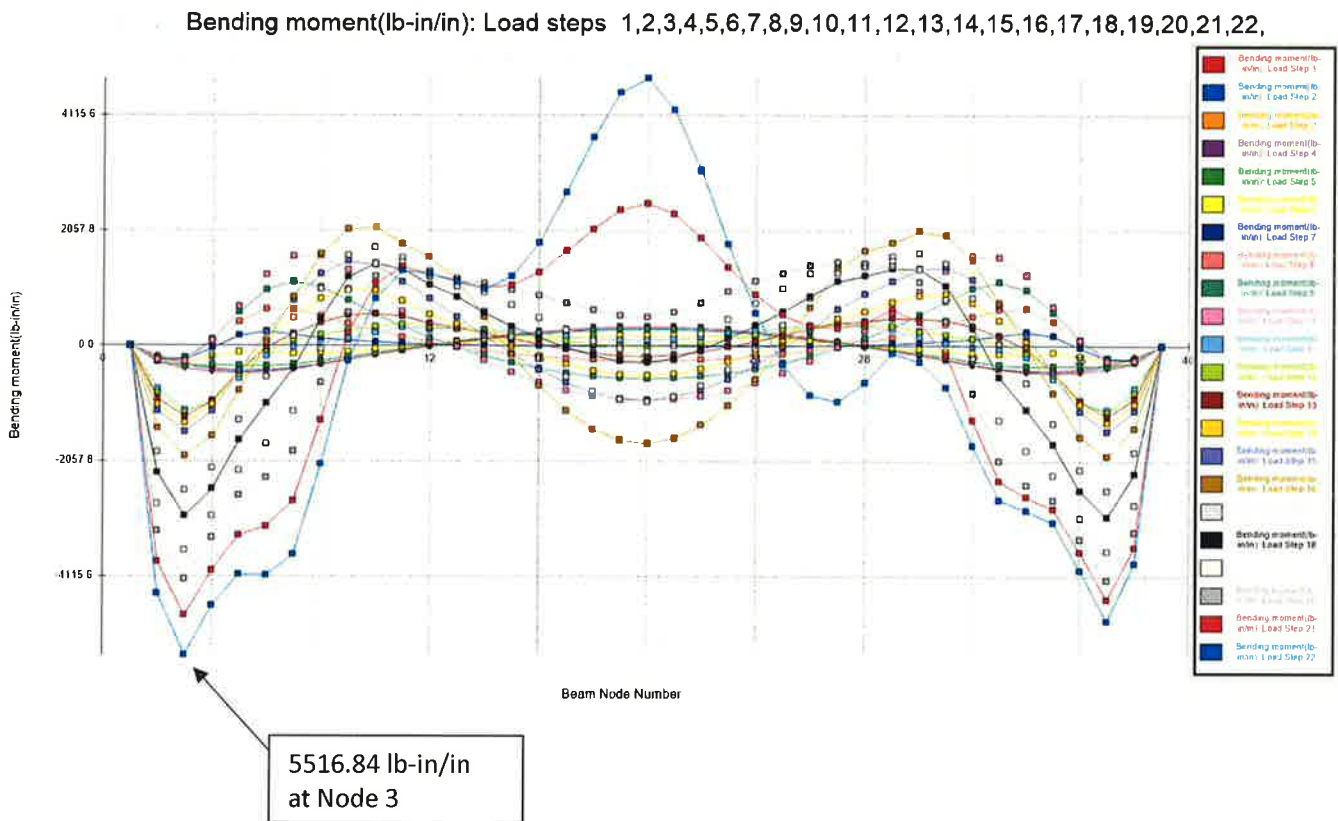
$$\text{Combined T\&M Ratio} = (T_f/R_t)^2 + M_u/M_n \leq 1.00$$

$$(\text{Factored thrust} / \text{Factored Thrust Resistance})^2 + (\text{Factored moment} / \text{Factored Moment Resistance}) \leq 1.00$$

The factored thrust resistance is the minimum yield point ( $F_y = 44,000$  psi) multiplied by the area of wall cross-section ( $0.2302 \text{ in}^2/\text{in}$  for 8 gage) multiplied by the plastic hinge resistance factor (0.90). The factored moment resistance is the plastic moment capacity ( $17660 \text{ lbs-in/in}$  for 8 gage) multiplied by the plastic hinge resistance factor. Refer to the NCSA Design manual (Table 2.14, pg. 37) for cross-section properties of BridgeCor.

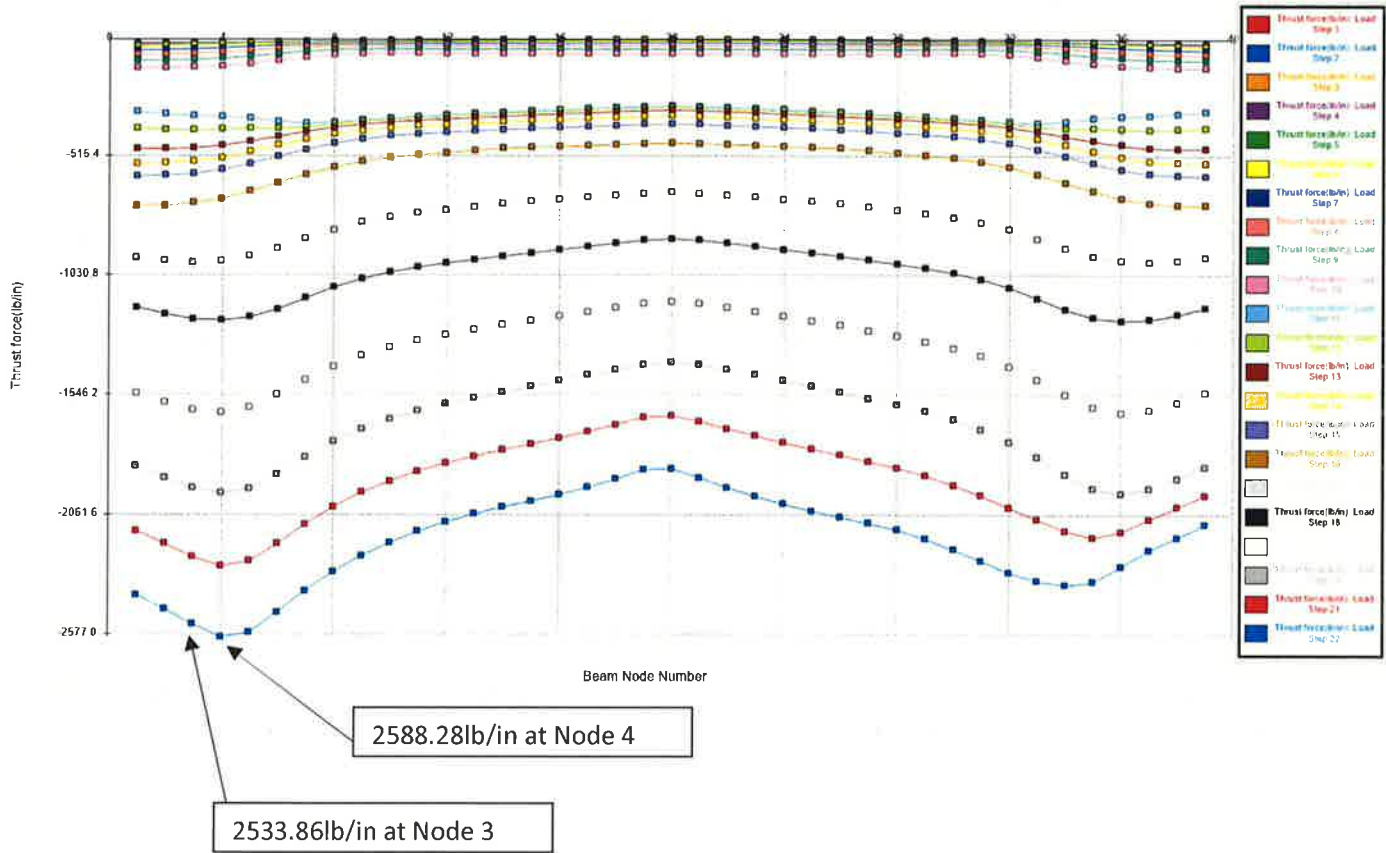
The following graphs show the bending moments and thrust forces along the cross-section of the BridgeCor structure. The x-axis correlates to the distance along the perimeter of the cross-section of the Two Radius Arch BridgeCor structure in inches.

$$\text{Combined Thrust \& Moment Ratio} = (2533.86 / (44,000 \times 0.2302 \times 0.90))^2 + (5516.84 / (17660 \times 0.90)) = 0.424 < 1.00 \text{ OK}$$





Thrust force(lb/in): Load steps 1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,



CANDE Controlling Node Output

NODE	X-COORD Y-COORD	X-DISP. Y-DISP.	N-PRES. S-PRES.	MOMENT THRUST	MAX-STRESS HOOP-STRESS	SHEAR S-STRESS
3	-192.08 28.58	-0.478E+00 -0.963E+00	-0.154E+02 -0.468E+01	-0.552E+04 -0.253E+04	-0.301E+05 -0.110E+05	0.613E+01 0.266E+02
4	-188.35 42.43	-0.489E+00 -0.965E+00	-0.270E+02 -0.345E+01	-0.464E+04 -0.259E+04	-0.273E+05 -0.112E+05	-0.506E+02 -0.220E+03

**AASHTO Section 12.8.9.6 (Global Buckling)** requires that the factored thrust in the culvert wall under the final installed condition shall not exceed the nominal resistance to general buckling capacity of the culvert, computed as:

$$R_b, \text{ nominal axial force in culvert wall to cause general buckling} = 1.2\Phi_b C_n (E_m I_p)^{1/3} (\Phi_s M_s K_b)^{2/3} R_h$$

- $\Phi_b$  , resistance factor for general buckling = 0.70
- $C_n$  , scalar calibration factor to account for some nonlinear effects = 0.55
- $E_m$  , modulus of elasticity of pipe wall material = 29000 ksi
- $I_p$  , moment of inertia of stiffened culvert wall per unit length= 0.875 in<sup>4</sup>/in
- $\Phi_s$  , resistance factor for soil = 0.9
- $\gamma$  , soil density = 120 pcf
- $R_{sp}$ , rise above springline= 131 inches
- $P_{sp} = 0.5\gamma R_{sp} = 4.55$  psi
- $M_s$  , constrained modulus of embedment computed = 2.53 ksi  
based on the free field vertical stress at a depth  
halfway between the top and springline of the  
structure (Table 12.12.3.5-1)
- $\nu$  , Poisson's ratio of soil = 0.30
- $K_b = (1-2\nu)/(1-\nu^2) = 0.44$
- $R_h$ , correction factor for backfill geometry = 11.4/(11+S/H) = 0.60
- S, culvert span = 382 inches
- H, depth of fill over top of culvert = 48 inches

$$R_b = 1.2 \times 0.70 \times 0.55 \times (29000 \times 0.875)^{1/3} (0.9 \times 2.53 \times 0.44)^{2/3} (0.60) = 8.17 \text{ kips/in}$$

$$R_b = 8.17 \text{ kips/in} > \text{Max Factored Buckling Thrust} = 2.58828 \text{ kips/in}$$

$$\text{Global Buckling Resistance Ratio} = 2.58828 / 8.17 = 0.317 < 1.00 \text{ OK}$$

**Table 12.12.3.5-1— $M_s$  Based on Soil Type and Compaction Condition**

$P_{sp}$ Stress Level (psi)	Sn-100 (ksi)	Sn-95 (ksi)	Sn-90 (ksi)	Sn-85 (ksi)
1.0	2.350	2.000	1.275	0.470
5.0	3.450	2.600	1.500	0.520
10.0	4.200	3.000	1.625	0.570
20.0	5.500	3.450	1.800	0.650
40.0	7.500	4.250	2.100	0.825
60.0	9.300	5.000	2.500	1.000
$P_{sp}$ Stress Level (psi)		Si-95 (ksi)	Si-90 (ksi)	Si-85 (ksi)

**AASHTO Section 12.7.2.3 (Wall Resistance)** requires the wall resistance to be greater than the factored thrust.

The wall resistance is defined as:

$$R_w = \Phi_w F_y A_w$$

$$A_w = \text{wall area (in}^2\text{/ft)} = 2.762 \text{ in}^2\text{/ft}$$

$$F_y = \text{yield strength of metal} = 44 \text{ ksi}$$

$$R_w = \Phi_w F_y A_w = 0.70 \times 44 \times 2.762 = 85.1 \text{ kips/ft} > \text{Max Factored Material Thrust} = 31.06 \text{ kips/ft}$$

$$\text{Wall Thrust Resistance Ratio} = 31.06 / 85.1 = 0.365 < 1.00 \text{ **OK**}$$

**AASHTO Section 12.7.2.5 (Seam Strength)** requires the factored seam strength to be greater than the factored thrust.

The factored seam strength is defined as:

$$R_s = \Phi_{SS} SS$$

$$\Phi_{SS}, \text{ Seam Strength} = 0.67 \text{ (AASHTO Table 12.5.5-1)}$$

$$SS = \text{Seam Strength} = 89 \text{ kips/ft (from Table 7.4B on page 376 of the NCSA Design Manual).}$$

$$R_s = 0.67 \times 89 = 59.63 \text{ kips/ft} > \text{Max Factored Seam Thrust} = 31.06 \text{ kips/ft}$$

$$\text{Seam Thrust Resistance Ratio} = 31.06 / 59.63 = 0.521 < 1.00 \text{ **OK**}$$

### CANDE Output Summary for controlling load step

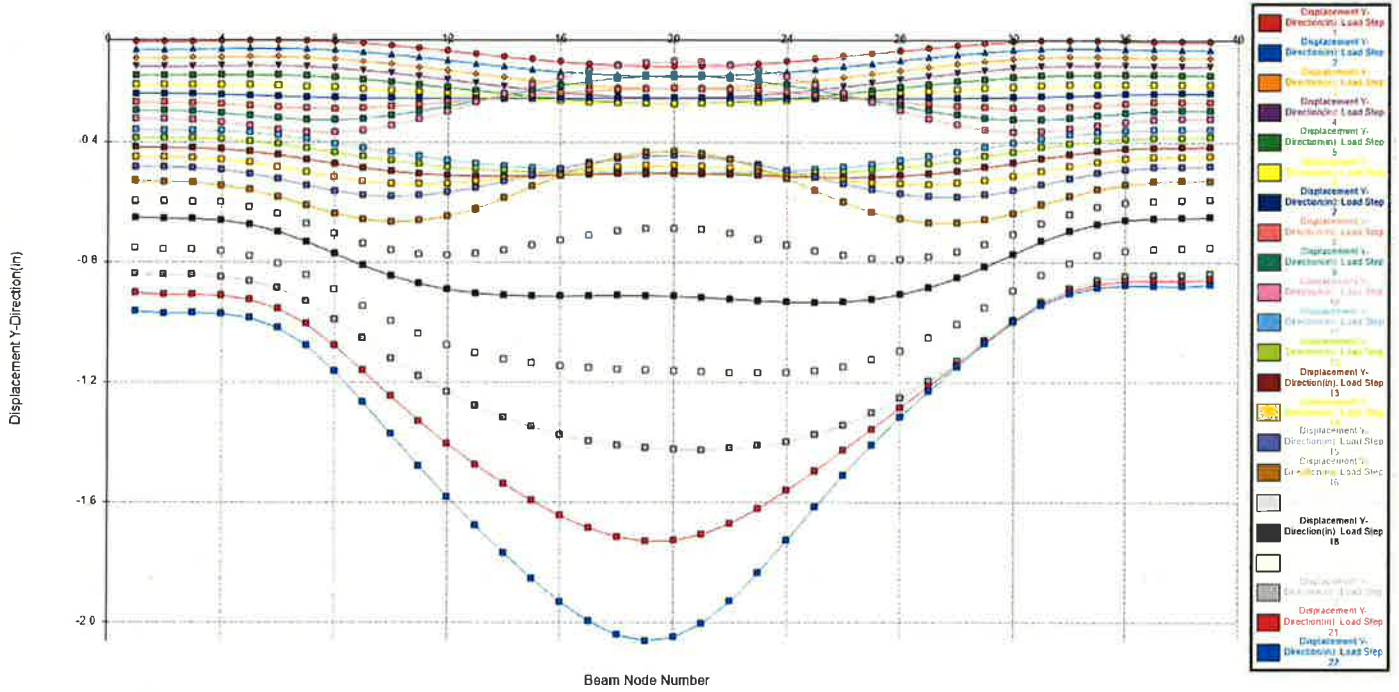
#### ASSESSMENT SUMMARY STEEL-GROUP 1, LOAD-STEP 22

LRFD STRENGTH-LIMIT RATIOS AT STEP 22, FOR STEEL GROUP # 1

DESIGN-CRITERION	CONTROL NODE	FACTORED DEMAND	FACTORED CAPACITY	RATIO VALUE
MATERIAL THRUST (psi)	4	11244.	30800.	0.365 < 1.00 <b>OK</b>
BUCKLING THRUST (psi)	4	11244.	53934.	0.208 < 1.00 <b>OK</b>
SEAM THRUST (psi)	4	11244.	21589.	0.521 < 1.00 <b>OK</b>
PLASTIC-PENETRATE (%)	0	0.00	90.00	0.000 < 1.00 <b>OK</b>
COMBINED T&M Ratio	3	0.423	1.000	0.423 < 1.00 <b>OK</b>



Displacement Y-Direction(in): Load steps 1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,



**CANDE OUTPUT FOR CONTROLLING LOAD STEP 22**

STRUCTURAL RESPONSES OF STEEL-GROUP 1, LOAD STEP 22

UNITS INCH-LB SYSTEM: (FORCE = LB/IN, MOMENT = IN-LB/IN, STRESS = PSI)

NODE	X-COORD Y-COORD	X-DISP. Y-DISP.	N-PRES. S-PRES.	MOMENT THRUST	MAX-STRESS HOOP-STRESS	SHEAR S-STRESS
1	-193.56 0.00	-0.351E+00 -0.957E+00	-0.917E+00 -0.295E+00	0.134E-10 -0.241E+04	-0.105E+05 -0.105E+05	0.422E+03 0.183E+04
2	-193.83 14.34	-0.428E+00 -0.964E+00	-0.816E+01 -0.249E+01	-0.442E+04 -0.247E+04	-0.261E+05 -0.107E+05	0.190E+03 0.826E+03
3	-192.08 28.58	-0.478E+00 -0.963E+00	-0.154E+02 -0.468E+01	-0.552E+04 -0.253E+04	-0.301E+05 -0.110E+05	0.613E+01 0.266E+02
4	-188.35 42.43	-0.489E+00 -0.965E+00	-0.270E+02 -0.345E+01	-0.464E+04 -0.259E+04	-0.273E+05 -0.112E+05	-0.506E+02 -0.220E+03
5	-182.71 55.62	-0.469E+00 -0.979E+00	-0.281E+02 0.516E+01	-0.408E+04 -0.257E+04	-0.253E+05 -0.112E+05	-0.187E+02 -0.813E+02
6	-175.27 67.89	-0.425E+00 -0.101E+01	-0.226E+02 0.676E+01	-0.410E+04 -0.248E+04	-0.250E+05 -0.108E+05	-0.109E+02 -0.476E+02
7	-166.18 78.98	-0.363E+00 -0.107E+01	-0.175E+02 0.522E+01	-0.373E+04 -0.239E+04	-0.233E+05 -0.104E+05	-0.665E+02 -0.289E+03
8	-155.61 88.69	-0.292E+00 -0.115E+01	-0.147E+02 0.472E+01	-0.212E+04 -0.231E+04	-0.174E+05 -0.100E+05	-0.119E+03 -0.516E+03
9	-144.43 97.10	-0.222E+00 -0.125E+01	-0.126E+02 0.369E+01	-0.277E+03 -0.224E+04	-0.107E+05 -0.972E+04	-0.102E+03 -0.443E+03
10	-132.78 104.87	-0.156E+00 -0.136E+01	-0.119E+02 0.347E+01	0.846E+03 -0.218E+04	-0.124E+05 -0.949E+04	-0.534E+02 -0.232E+03
11	-120.72 111.98	-0.990E-01 -0.147E+01	-0.113E+02 0.327E+01	0.134E+04 -0.213E+04	-0.139E+05 -0.927E+04	-0.112E+02 -0.487E+02
12	-108.28 118.40	-0.517E-01 -0.157E+01	-0.876E+01 0.255E+01	0.128E+04 -0.209E+04	-0.135E+05 -0.909E+04	0.113E+02 0.490E+02
13	-95.50 124.11	-0.137E-01 -0.166E+01	-0.808E+01 0.236E+01	0.114E+04 -0.206E+04	-0.129E+05 -0.894E+04	0.137E+02 0.596E+02
14	-82.42 129.10	0.161E-01 -0.175E+01	-0.630E+01 0.184E+01	0.102E+04 -0.203E+04	-0.123E+05 -0.882E+04	0.656E+00 0.285E+01

15	-69.09 133.35	0.386E-01 -0.184E+01	-0.601E+01 0.175E+01	0.124E+04 -0.200E+04	-0.130E+05 -0.870E+04	-0.253E+02 -0.110E+03
16	-55.53 136.84	0.542E-01 -0.192E+01	-0.627E+01 0.183E+01	0.184E+04 -0.198E+04	-0.150E+05 -0.858E+04	-0.500E+02 -0.217E+03
17	-41.80 139.57	0.630E-01 -0.198E+01	-0.723E+01 0.212E+01	0.274E+04 -0.194E+04	-0.179E+05 -0.845E+04	-0.645E+02 -0.280E+03
18	-27.94 141.53	0.656E-01 -0.203E+01	-0.842E+01 0.247E+01	0.372E+04 -0.191E+04	-0.212E+05 -0.829E+04	-0.621E+02 -0.270E+03
19	-13.99 142.70	0.636E-01 -0.205E+01	-0.101E+02 0.294E+01	0.452E+04 -0.187E+04	-0.238E+05 -0.812E+04	-0.378E+02 -0.164E+03
20	0.00 143.09	0.598E-01 -0.203E+01	-0.114E+02 -0.240E+01	0.477E+04 -0.186E+04	-0.246E+05 -0.810E+04	0.864E+01 0.376E+02
21	13.99 142.70	0.573E-01 -0.199E+01	-0.102E+02 -0.295E+01	0.421E+04 -0.190E+04	-0.229E+05 -0.827E+04	0.548E+02 0.238E+03
22	27.94 141.53	0.597E-01 -0.192E+01	-0.875E+01 -0.255E+01	0.312E+04 -0.195E+04	-0.193E+05 -0.845E+04	0.801E+02 0.348E+03
23	41.80 139.57	0.689E-01 -0.182E+01	-0.739E+01 -0.216E+01	0.181E+04 -0.198E+04	-0.149E+05 -0.861E+04	0.839E+02 0.365E+03
24	55.53 136.84	0.858E-01 -0.171E+01	-0.651E+01 -0.190E+01	0.586E+03 -0.202E+04	-0.108E+05 -0.876E+04	0.700E+02 0.304E+03
25	69.09 133.35	0.110E+00 -0.160E+01	-0.623E+01 -0.182E+01	-0.341E+03 -0.205E+04	-0.101E+05 -0.889E+04	0.463E+02 0.201E+03
26	82.42 129.10	0.139E+00 -0.150E+01	-0.610E+01 -0.179E+01	-0.887E+03 -0.207E+04	-0.121E+05 -0.900E+04	0.180E+02 0.781E+02
27	95.50 124.11	0.172E+00 -0.140E+01	-0.619E+01 -0.182E+01	-0.994E+03 -0.210E+04	-0.126E+05 -0.912E+04	-0.121E+02 -0.527E+02
28	108.28 118.40	0.208E+00 -0.131E+01	-0.751E+01 -0.220E+01	-0.663E+03 -0.213E+04	-0.115E+05 -0.923E+04	-0.338E+02 -0.147E+03
29	120.72 111.98	0.247E+00 -0.122E+01	-0.122E+02 -0.357E+01	-0.130E+03 -0.217E+04	-0.986E+04 -0.941E+04	-0.155E+02 -0.674E+02
30	132.78 104.87	0.290E+00 -0.114E+01	-0.104E+02 -0.306E+01	-0.283E+03 -0.221E+04	-0.106E+05 -0.961E+04	0.207E+02 0.900E+02

31	144.43 97.10	0.3336E+00 -0.106E+01	-0.121E+02 -0.355E+01	-0.742E+03 -0.226E+04	-0.124E+05 -0.982E+04	0.535E+02 0.232E+03
32	155.61 88.69	0.383E+00 -0.993E+00	-0.155E+02 -0.289E+01	-0.179E+04 -0.231E+04	-0.163E+05 -0.100E+05	0.710E+02 0.309E+03
33	166.18 78.98	0.429E+00 -0.936E+00	-0.194E+02 -0.107E+01	-0.275E+04 -0.235E+04	-0.197E+05 -0.102E+05	0.409E+02 0.178E+03
34	175.27 67.89	0.467E+00 -0.898E+00	-0.233E+02 -0.881E+00	-0.295E+04 -0.237E+04	-0.205E+05 -0.103E+05	0.150E+02 0.653E+02
35	182.71 55.62	0.492E+00 -0.878E+00	-0.263E+02 0.345E+01	-0.315E+04 -0.235E+04	-0.211E+05 -0.102E+05	0.383E+02 0.166E+03
36	188.35 42.43	0.497E+00 -0.871E+00	-0.227E+02 0.684E+01	-0.401E+04 -0.229E+04	-0.238E+05 -0.993E+04	0.628E+02 0.273E+03
37	192.08 28.58	0.475E+00 -0.872E+00	-0.124E+02 0.377E+01	-0.491E+04 -0.221E+04	-0.266E+05 -0.962E+04	-0.244E+01 -0.106E+02
38	193.83 14.34	0.419E+00 -0.875E+00	-0.743E+01 0.225E+01	-0.388E+04 -0.216E+04	-0.228E+05 -0.939E+04	-0.169E+03 -0.733E+03
39	193.56 0.00	0.338E+00 -0.869E+00	-0.243E+01 0.734E+00	-0.331E-10 -0.211E+04	-0.914E+04 -0.914E+04	-0.367E+03 -0.160E+04